

- The motion of a particle in  $XY$  plane is  $\mathbf{r}(t)=(1+\cos 2t, 2+\sin 2t)$ , SI units. a) Find the velocity  $\mathbf{v}(t)$  and the acceleration  $\mathbf{a}(t)$ . b) Find the value for  $\mathbf{v}(1)$  and  $\mathbf{a}(1)$ . c) Find the intrinsic components of the acceleration,  $\bar{a}_t(t)$  and  $\bar{a}_n(t)$ . d) Determine the trajectory of the particle.  
**Ans.:** a)  $\mathbf{v}(t)=(-2\sin 2t, 2\cos 2t)$ ,  $\mathbf{a}(t)=(-4\cos 2t, -4\sin 2t)$ ; b)  $\bar{v}(1)=(-1,819, -0,832)$  m/s;  $\bar{a}(1)=(1,67;3,64)$  m/s<sup>2</sup>; c)  $\bar{a}_t(t)=0$ ;  $\bar{a}_n(t)=\bar{a}(t)$  (m/s<sup>2</sup>);  $(x-1)^2+(y-2)^2=1$   $\equiv$  A circumference with radius 1 m and center in point (1, 2)
- The components of the position vector of a body moving in the  $XY$  plane are:  $x=16t+2t^2$ ,  $y=18t-1,5t^2$ , SI units. At  $t=1$  s, calculate: a) Cartesian coordinates and intrinsic components of the acceleration. b) The unit vectors  $\mathbf{u}_t$  and  $\mathbf{u}_n$ , showing that they are perpendicular to each other. c) The position of the center of curvature.  
**Ans.:** a)  $a_x=4$  m/s<sup>2</sup>;  $a_y=-3$  m/s<sup>2</sup>;  $a_t=1,4$  m/s<sup>2</sup>;  $a_n=4,8$  m/s<sup>2</sup>; b)  $\mathbf{u}_t=(0,8, 0,6)$ ;  $\mathbf{u}_n=(0,6, -0,8)$ ; c) C.C:  $x=96,12$  m,  $y=-87,67$  m
- A particle is moving in  $XY$  plane with  $a_x=0$ ,  $a_y=5$  m/s<sup>2</sup>. At  $t=0$  the position is  $x=0$ ,  $y=8$  m, and the velocity is  $v_x=5$ ,  $v_y=0$  m/s. Determine: a) The law of motion  $\bar{r}(t)$ ; b) the equation of the trajectory; c) the intrinsic components of the acceleration at  $t=1$  s. **Ans.:**  $r(t)=(5t, 8+5/2 \cdot t^2)$ ;  $y=8+x^2/10$ ;  $a_t(1)=5/\sqrt{2}$  ms<sup>-2</sup>;  $a_n(1)=5/\sqrt{2}$  ms<sup>-2</sup>.
- An iron sphere is dropped and allowed to fall freely from a balcony. It takes to it 0,10 s for going through the last meter. a) What is the initial height? b) What is the final speed? **Ans.:** a) 5,5 m; b) 10,5 m/s
- A stone is thrown vertically upwards and is 10 s in the air. Neglecting the air resistance and taking  $g=10$  m/s<sup>2</sup>, calculate the initial throwing speed and the maximum height the stone reaches. **Ans.:** 50 m/s; 125 m.
- A child throws horizontally a ball from a balcony at height  $y_0$ , with an initial speed  $v_0$ . At the same instant, another child on the street throws another ball vertically with speed  $2v_0$ , from a point located at distance  $d$  from the first building. Find the value of  $d$  for making the balls to collide to each other. **Ans.:**  $d=y_0/2$
- When a stone is thrown with speed  $v_0$  at an angle  $\alpha$ , it hits the ground at a distance of 50 m (neglecting the air resistance). If the same stone is thrown at the same angle but with speed  $2v_0$ , which is the range? **Ans.:** 200 m
- A ball is thrown vertically upwards with an initial speed of 20 m/s from the roof of a building 50 m tall. The ball is pushed by the wind, with an horizontal acceleration of 2 m/s<sup>2</sup>. Taking  $g=10$  m/s<sup>2</sup>, calculate: a) Horizontal distance between the initial point and the point of impact. b) Maximum height. c) Intrinsic components of the acceleration when the ball reaches 60 m above ground the first time. **Ans.:** a) 32,97 m; b) 70 m; c)  $a_t=-9,02$  m/s<sup>2</sup>;  $a_n=4,32$  m/s<sup>2</sup>.
- William Tell aims to the apple atop his son's head, at a distance  $d$  and 50 cm below from shooting position. The initial speed of the arrow is 50 m/s, with an angle 30°. The wind produces an horizontal acceleration of 2 m/s<sup>2</sup>, braking the arrow. Taking  $g=10$  m/s<sup>2</sup>, calculate: a) Horizontal distance  $d$  required for the arrow to go through the apple; b) Maximum height the arrow reaches, as measured from point of shooting. **Ans.:** a) 192,4 m; b) 31,3 m
- See figure. A body is thrown from a point P in the slope (22°) of a hill. The initial speed is  $v_0=150$  m/s, forming an angle of 31° with respect to the mountainside (see figure). Calculate the flight time, the distance from P when it hits the ground and the speed at this point of impact.  $g=10$  m/s<sup>2</sup>. **Ans.:**  $t=16,8$ s;  $d=1628$  m;  $v_x=90$  m/s,  $v_y=-48$  m/s,  $v=102$  m/s
- A circular platform with radius 2 m, initially at rest, start to rotate with an angular acceleration 1,5 rad/s<sup>2</sup>, kept constant for 4 secs. Later on, the angular speed is kept constant for half minute. Finally, the platform brakes and stops in 3 secs. Calculate: a) Number of revolutions; b) Distance covered by a point in the periphery; c) linear velocity, tangential acceleration and normal acceleration for a point in the periphery at  $t_1=2$  s,  $t_2=20$  s and  $t_3=35$  s. **Ans.:** a) 32 rounds; b) 402 m; c)  $v(2)=6$  m/s,  $a_t(2)=3$  m/s<sup>2</sup>,  $a_n(2)=18$  m/s<sup>2</sup>;  $v(20)=12$  m/s;  $a_t(20)=0$ ,  $a_n(20)=72$  m/s<sup>2</sup>;  $v(35)=8$  m/s,  $a_t(35)=-4$  m/s<sup>2</sup>;  $a_n(35)=32$  m/s<sup>2</sup>

